



THE UNIVERSITY OF TEXAS AT EL PASO

Recursion

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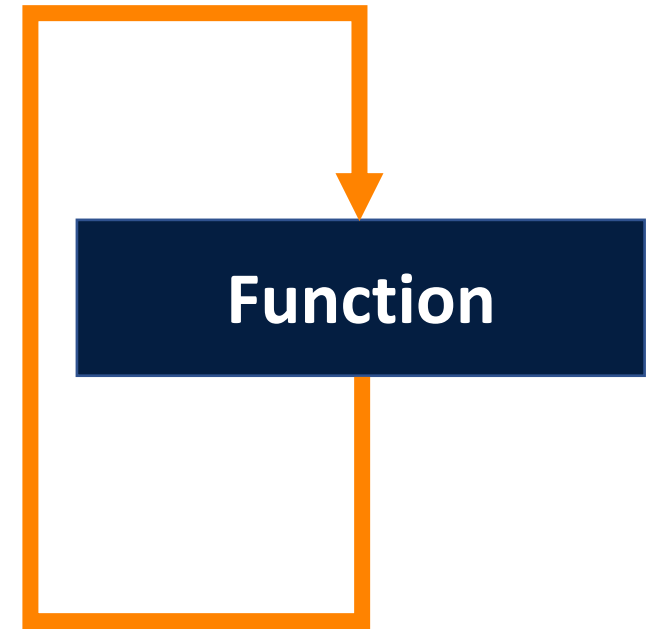
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What is Recursion?

- Recursion is fundamental technique in Computer Science and can be applied to tasks that are **repetitive**.
- Recursion is a function that **calls itself**.
- Recursion is generally used when a problem can be **divided into smaller part**.



Which tasks we can apply recursion?

1. Repetitive Tasks

2. Divided into smaller part

Any Ideas from students?

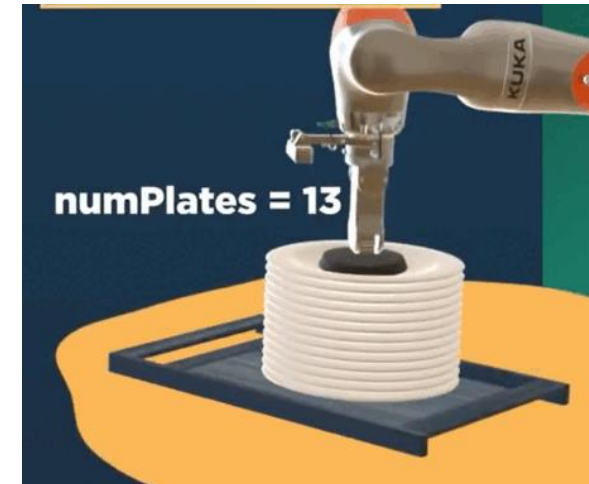
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Timer

Program for factorial of a number

$$n! = n * (n-1) * (n-2) * \dots * 1$$
$$4! = 4 * 3 * 2 * 1 = 24$$
$$6! = 6 * 5 * 4 * 3 * 2 * 1 = 720$$

Mathematical Factorial



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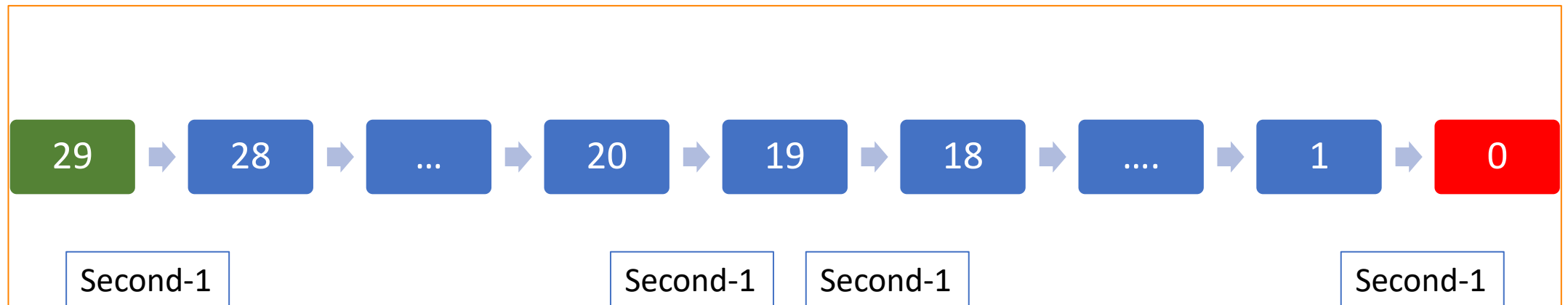
Timer – How can we divided into subtask?

0:30

Timer

Pseudocode:

1. Print (second -1) after each second passes
2. Stop the timer when it reaches 0



2. Stop/Base Case

1. Recursive Case



Recursive Solutions

When creating a recursive solution, there are a few things we want to keep in mind:

1. We need to break the problem into **smaller pieces** of itself
2. We need to define a “**base case**” to stop at
3. The smaller problems we **break down** into need to eventually reach the base case

How Recursion Function is Developed

```
def timerRecursive(seconds):
```

Base Case

Recursion ends and returns a value/exit

Recursive Case

Function call itself

Sample Recursion code Run: <https://onlinegdb.com/LV76WYXxc>

Recursion Terminology

```
def func(n):  
    if n == 0:  
        return 0  
  
    print(n)  
    return func(n - 1)
```

Base case

Recursive case

Task: Find func(5)

func(5)

Print(5)
return func(4)

func(4)

Print(4)
return func(3)

func(3)

Print(3)
return func(2)

func(2)

Print(2)
return func(1)

func(1)

Print(1)
return func(0)

func(0)

return 0

Recursion Issue

```
def func(n):  
    if n == 0:  
        return 0  
  
    print (n)  
    return func (n + 1)
```

Find `func(5)`

We have a base case and a recursive case.

What's wrong?

Recursion Issue

```
def func(n):  
    if n == 0:  
        return 0  
  
    print (n)  
    return func (n + 1)
```

Find func(5)

func(5)

Print(5)
return func (6)

func(6)

Print(6)
return func (7)

func(7)

Print(7)
return func (8)

func(8)

Print(8)
return func (9)

...

func(1000)

Print(1000)
return func (1001)

Recursion Issue

```
def func(n):  
    if n == 0:  
        return 0  
  
    print (n)  
    return func (n + 1)
```

Find func(5)

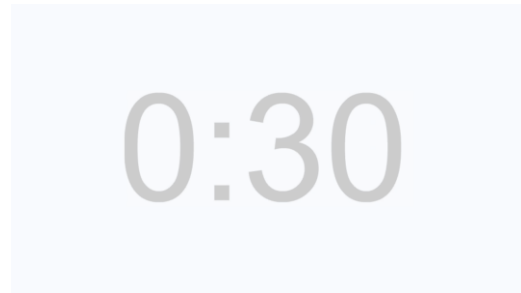
```
def func(n):  
    if n == 0:  
        return 0  
  
    print (n)  
    return func (n - 1)
```

Find func(5)

Important when you code

1. Make Sure **base case** is called at some point
2. Try to avoid forever loop
3. **Recursive cases** will end up with **base case** at some point

Which tasks we can apply recursion?

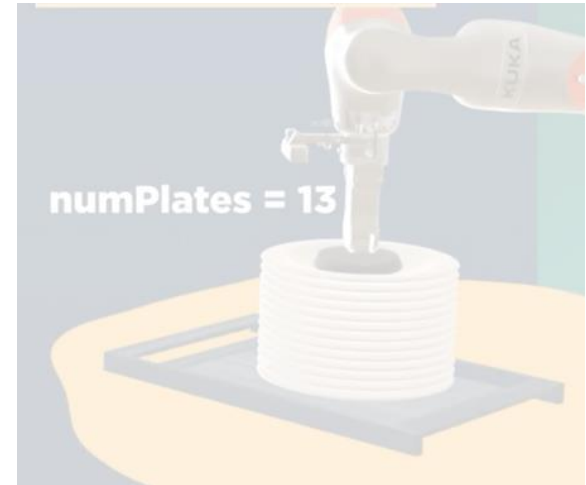


Timer

```
Program for factorial of a number  
  
n! = n * (n-1) * (n-2) * ..... *1  
4! = 4*3*2*1 = 24  
6! = 6*5*4*3*2*1 = 720
```

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Mathematical Factorial



Robot Put Away Plates

Mathematical Factorial

- Does anyone know the **value of 9!** ?
- 362,880
- Does anyone know the **value of 10!** ?
- How did you know?

Mathematical Factorial

$$9! = 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$

$$10! = 10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1$$

$$10! = 10 \times 9!$$

$$n! = n \times (n - 1)!$$

That's a recursive definition!

Mathematical Factorial

Step 1:

$$n! = n \times (n - 1)!$$

Step 2:

```
def fact(n):  
    return n * fact(n - 1)
```

Step 3:

```
fact(3)  
3 * fact(2)  
3 * 2 * fact(1)  
3 * 2 * 1 * fact(0)  
...
```

Mathematical Factorial

What did we do wrong?

Missing base case for recursion

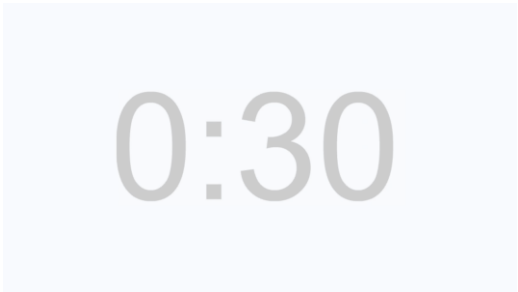
```
def fact(n):  
    return n*fact(n-1)
```

Find fact(10)

```
def fact(n):  
    if n == 1:  
        return 1  
  
    return n*fact(n-1)
```

Find fact(10)

Which tasks we can apply recursion?



Timer

```
Program for factorial of a number  
  
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```

Mathematical Factorial



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Robot Put Away Recursion Code

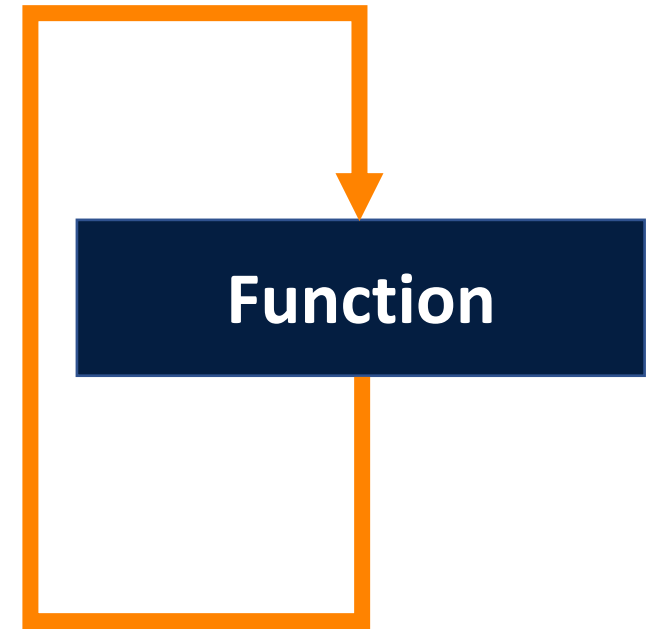
```
def putAwayPlate(numberPlates) :  
  
    if numberPlates == 0:  
        print ("Finished")  
        return 0;  
  
    movePlate()  
    putAwayPlate(numberPlates - 1)
```



Robot Put Away Plates

Summary

- Recursion is fundamental technique in Computer Science and can be applied to tasks that are **repetitive**.
- Recursion is a function that **calls itself**.
- Recursion has 2 cases
 - Recursive cases
 - Stop/base case
- Make Sure **base case** is called at some point
- Try to avoid forever loop



Any Questions

0:30

Timer

Program for factorial of a number

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Mathematical Factorial



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